



**NTNU – Trondheim**  
Norwegian University of  
Science and Technology

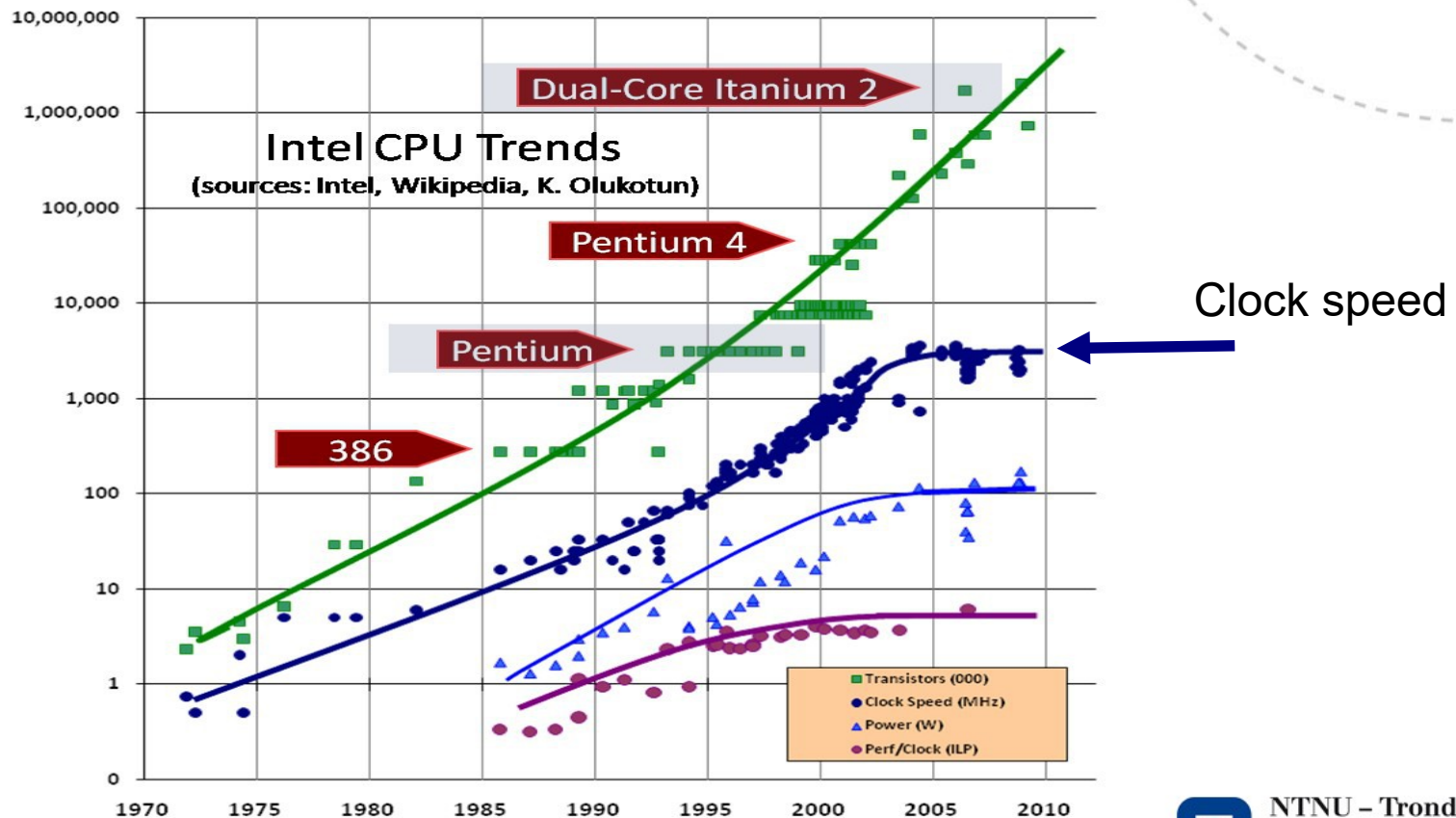
## **Agenda**

1. CPU History
2. Compiler optimization
3. Cache
4. Libraries
5. Memory allocation

[www.hpc.ntnu.no](http://www.hpc.ntnu.no)

# CPU HISTORY

- Moore's law (1965): Number of transistores doubles every two years.
- The clock frequency has flat out since 2005.



## CPU energy consumption

CPU Transistor effect:  $P \sim C * F * U^2$

C: Capacitance , F: Frequency , U: Transistor voltage

### Dennard scaling law (1974):

Transistors get smaller and power density stays constant

Dannard law	(new vs old cpu)	Today
$L_{new} = L / 2$	(transistor length)	$L_{new} = L / 2$
$D_{new} = 1 / L^2 = 4D$	(Density)	$D_{new} = 4D$
$U_{new} = U / 2$	(Voltage)	$U_{new} \sim U$ (same voltage)
$F_{new} = 2 * F$	(Frequency)	$F_{new} = 2 * F$
$P_{new} = P$	(Power)	$P_{new} = 4P$

(POWER CRISES IF THE FREQUENCY INCREASE!!!)

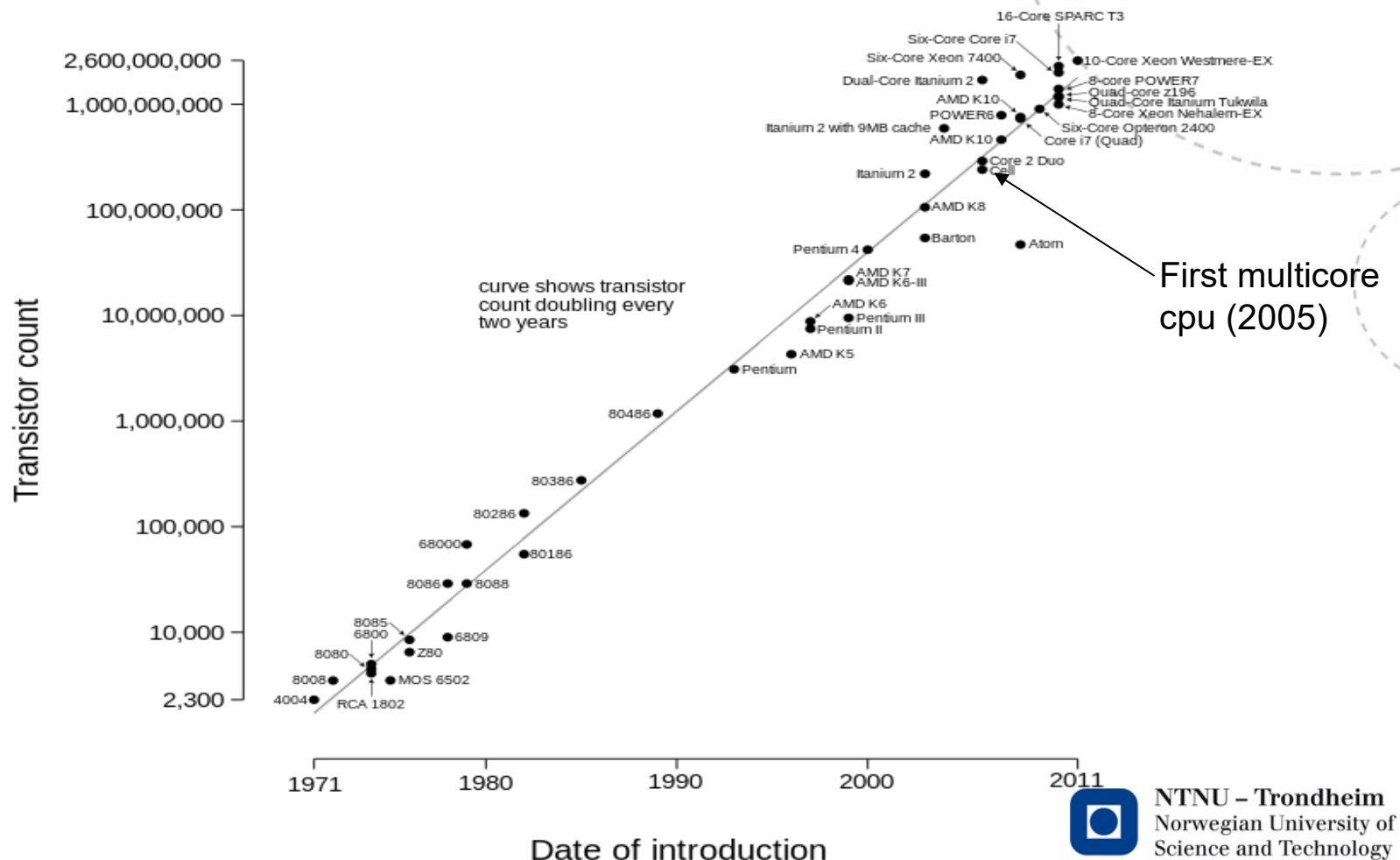
- The transistor voltage can not be decreased much more.
- Transistor temperature and power can not increase.
- CPU frequency can not increase much more.
- Dennard scaling law do not hold anymore.



# Moore's Law and number of cores

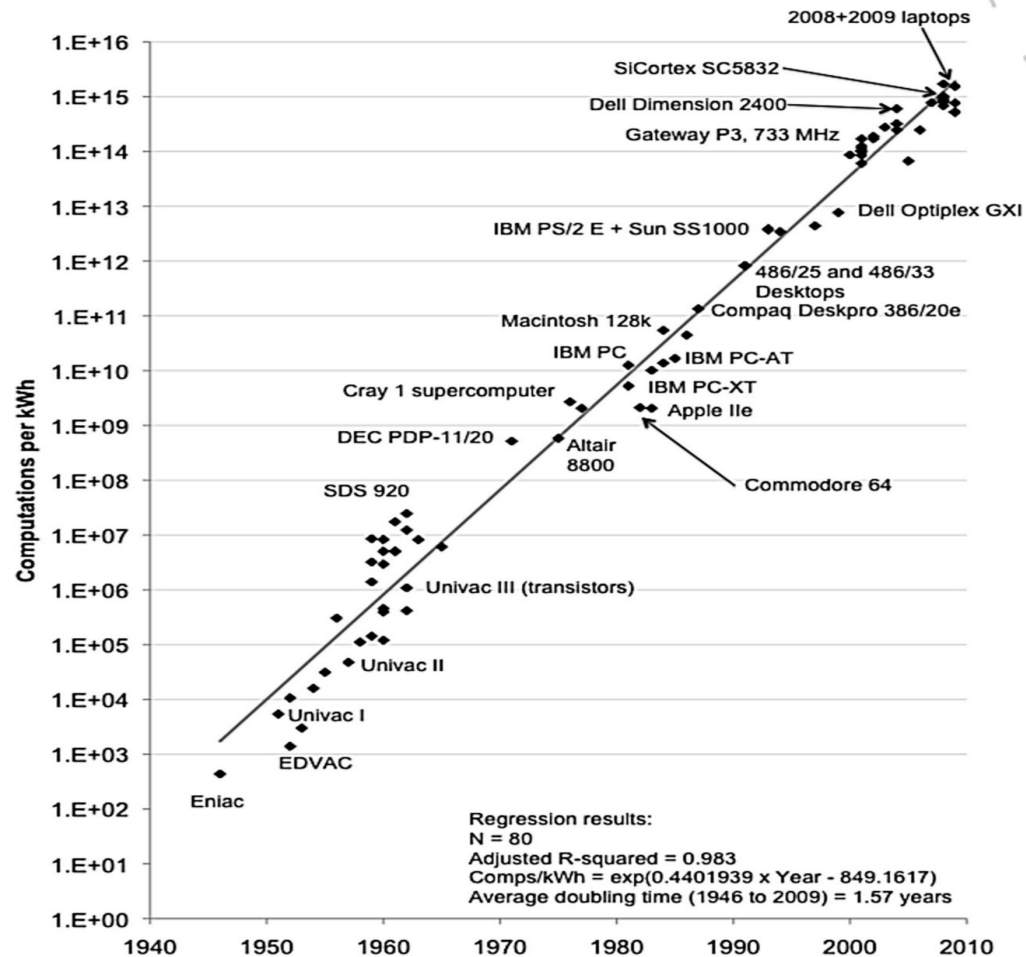
Number of transistors double every 1.8 years. Moore's law still hold

## Microprocessor Transistor Counts 1971-2011 & Moore's Law



# Koomey's performance law:

Computation per watt has been doubling every 1.57 years



## Vilje (SGI Altix 8600)

	Each Node	Total
Cores	16	23040
Nodes	-	1440
Memory	32GB	46TB
Storage	-	1000TB
Flops		479 Tflops (peak)

## Lille (Dell)

	Each Node	Total
Cores	20	520
Nodes	-	27
Memory	128GB	3.4 TB



# Compiler optimization

```
icc -O2 -o myprogram myprogram.c
```

See compiler options: `man icc`. Fortran **ifort**

The optimization code **-O2** is default

(Note! For gnu compiler; use `gcc -O2 ....`)

Optimization code:

**O0**: Optimization is disabled

**O1**: Enables optimizations for speed and disables some optimizations that increase code size and affect speed.

**O2**: Enables optimizations for speed (default). This is the generally recommended optimization level. Vectorization is enabled at O2 and higher levels.

**O3**: Enables O2 optimizations plus more aggressive optimization.

**AVX**: Intel AVX vector extension (only for icc) (Sandy bridge and newer processors )  
(See [http://en.wikipedia.org/wiki/Advanced\\_Vector\\_Extensions](http://en.wikipedia.org/wiki/Advanced_Vector_Extensions))

```
icc -O3 -xAVX -o myprogram myprogram.c    (gcc: -mavx or -mpku)
```

**Parallel**: Automatically parallelizing of the code, with `-parallel` as (not on gcc):

```
icc -O3 -parallel -o myprogram myprogram.c    (gcc: ftree-parallelize-loops=n)
```

**Fast**: The `-fast` option maximizes speed across the entire program. Longer compiling time.

```
icc -O3 -fast -o myprogram myprogram.c
```



## Results Lille (gcc compiler)

	-O0	-O1	-O2	-O3	-O3 -xAVX	-O3 -parallel
arrav1	14.8 s	5.1s	5.1s	4.55s		
pi	12.3s	4.8s	4.8s	4.8s		

## Results Vilje (Intel compiler)

	-O0	-O1	-O2	-O3	-O3 -xAVX	-O3 -parallel
arrav1	28.1s	10.8s	3.6s	0.98s	0.49s	1.1s
pi	18.4s	8.5s	4.3s	4.2s	4.2s	0.3s

```

Pi: for(i=0;i<nsteps;i++){
        x = (i + 0.5) * step;
        sum += 4.0/(1.0 + x * x);
    }
nsteps=10^9
  
```

```

Array1: for (t=0;t<T;t++)
            for (i=0;i<n;i++)
                C[i]+=A[i]*B[i];
  
```

n=10<sup>6</sup>, T=5000



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# CACHE

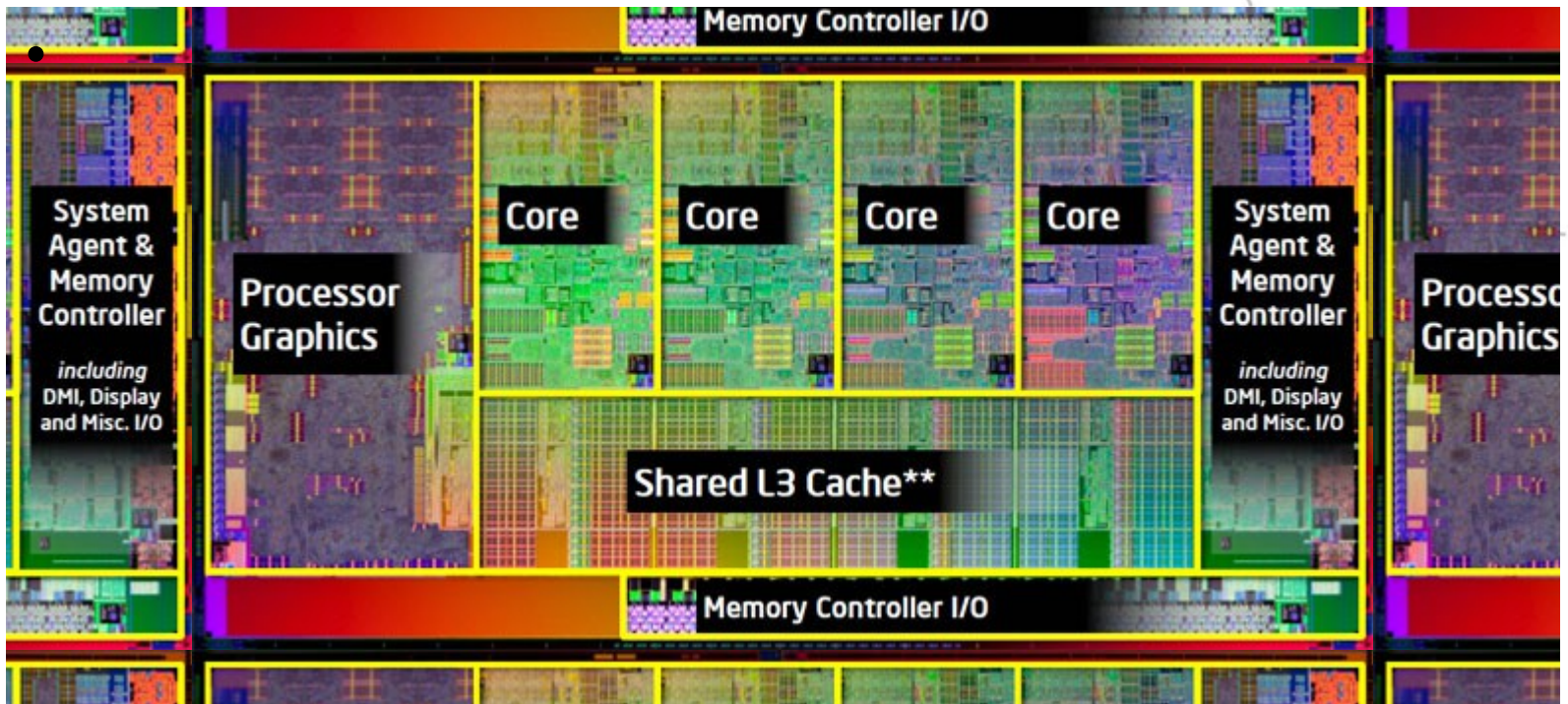


Fig. Laptop/pc CPU (Intel i7) with 4 cores

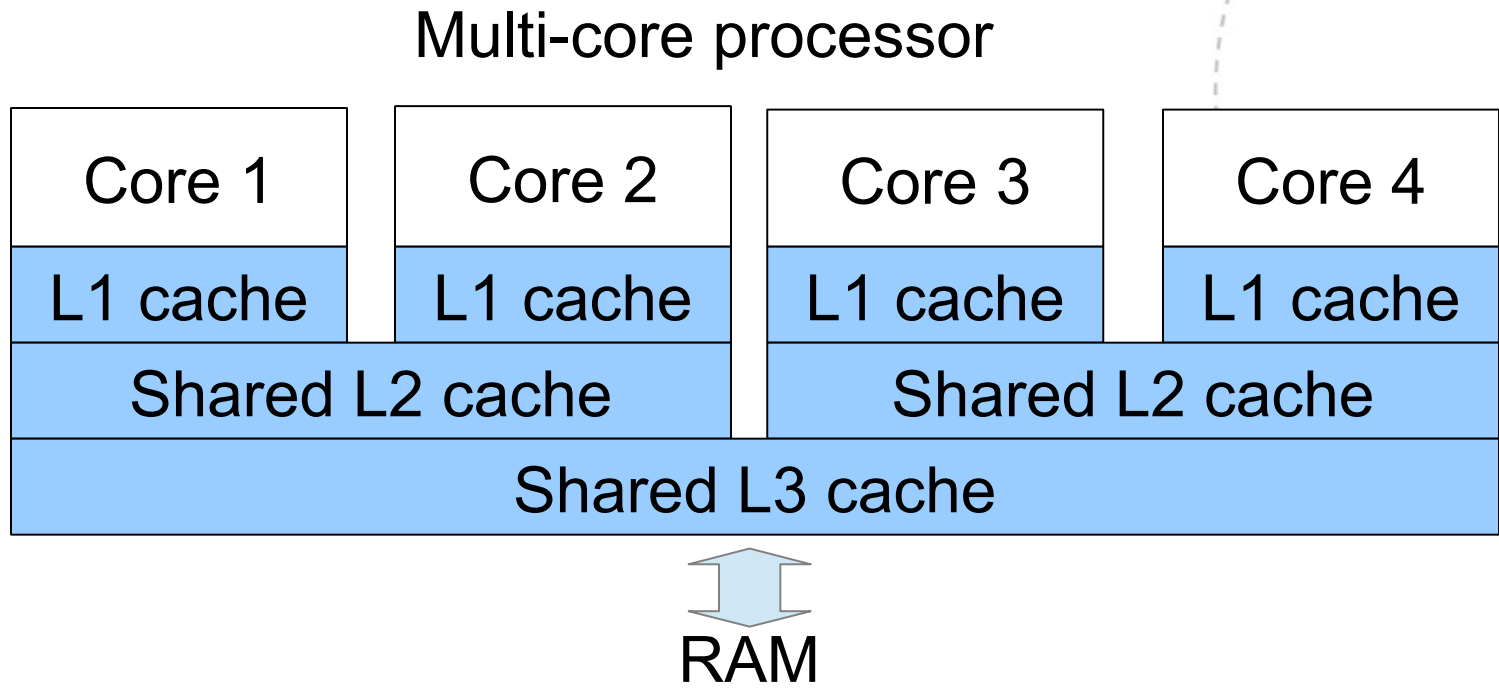


Figure 1. Intel i7 Sandy Bridge, 4 core processor with cache memory.  
 ( L1: 64kB ~4cycles, L2: 256kB ~10cycles, L3: up to 20MB ~40cycles, RAM 32GB~120cycles)

- Each core has small memory cache L1 (level 1).
- Level 2 and 3 cache are shared between cores

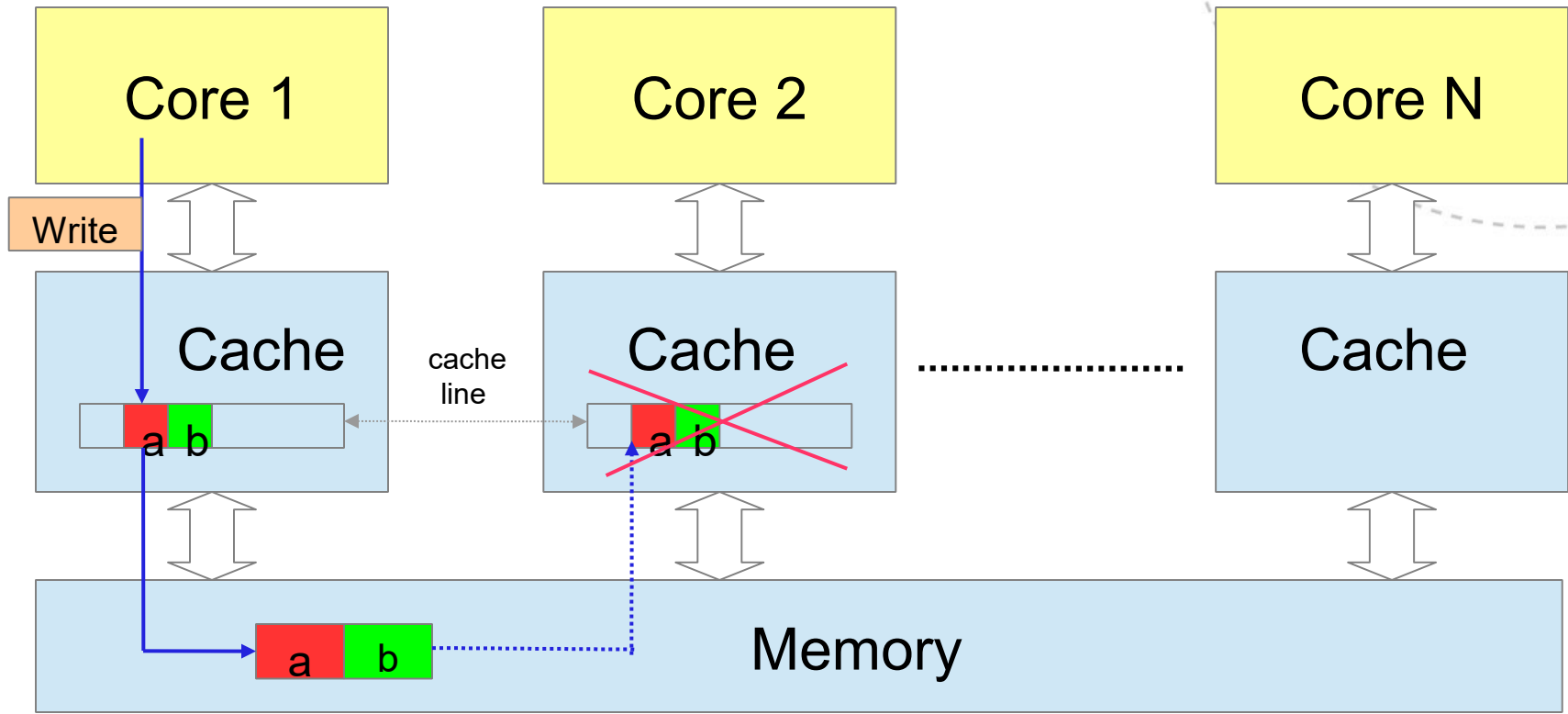
# False Sharing

(See [http://en.wikipedia.org/wiki/False\\_sharing](http://en.wikipedia.org/wiki/False_sharing))

The memory addresses are grouped into cache lines.

If one element in the cache line is changed of one core; the whole line will be automatically synchronized with the other cores cache. Drawback is that this will slow down because of data update latency.

# False Sharing.



## Cache miss

Cache miss is a state where the data requested for processing by a component or application is not found in the cache memory. It causes execution delays by requiring the program or application to fetch the data from other cache levels or the main memory.

### Example that can cause cache miss

```
for (i=0; i<N; i++)  
    A[i] += A[i-1]*A[i+1];
```

## Cache miss: Example codes (for loop)

```
int i,j,N=5000;
float data[N][N];
```

### Code A

```
for (i=0;i<N;i++)
  for (j=0;j<N;j++)
    data[i][j]=i*j;
```

...

### Code B

```
for (i=0;i<N;i++)
  for (j=0;j<N;j++)
    data[j][i]=i*j; //Give lot of false sharing
```

(Note! The indexing is opposite for Fortran)

Vilje: (j,i) 1.48s (i,j) 0.75s      Idun: (j,i):3,1s (i,j) 0.36s



## Example of avoiding cache misses

A, B and C arrays of type double and N elements.

```
for (i=0;i<N;i++)  
    C[i] += A[i]*A2[i];
```

Divide forloop in to blocks of cache line size

If cache size = 64kB

```
int blocksize=64000/sizeof(double);
```

```
for (i=0;i<n;i+=blocksize)  
    for (block=0;block<blocksize;block++)  
        C[i+block] += A[i+block] * B[i+block];
```



# LIBRARIES

## Intel MKL Components (Lille: OpenBLAS)

### Linear Algebra

BLAS • LAPACK/ ScaLAPACK • PARDISO\* • Iterative sparse solvers

### Fast Fourier Transforms

Multidimensional (up to 7D) FFTs • FFTW interfaces • Cluster FFT

### Summary Statistics

Kurtosis • Variation coefficient • Quantiles, order statistics • Min/max • Variance/ covariance • ...

### Data Fitting

Splines • Interpolation • Cell search

### Other Components

Vector Math • Trigonometric • Hyperbolic • Exponential, Logarithmic • Power/Root Rounding • Vector Random Number Generators • Conguential • Recursive • WichmannHill • Mersenne Twister • Sobol • Neiderreiter • RDRANDbased • Poisson Solvers • Optimization Solvers





## Example: Matrix multiplication with MKL library `cblas_dgemm` Multiply Matrices Using `dgemm`

$$\mathbf{C} \leftarrow \alpha \mathbf{A} * \mathbf{B} + \beta \mathbf{C}$$

```
cblas_dgemm(CblasRowMajor, CblasNoTrans, CblasNoTrans,  
            m, n, k, alpha, A, k, B, n, beta, C, n);
```

The arguments provide options for how Intel MKL performs the operation. In this case:

`CblasRowMajor`: Indicates that the matrices are stored in row major order, with the elements of each row of the matrix stored contiguously as shown in the figure above.

`CblasNoTrans`: Enumeration type indicating that the matrices A and B should not be transposed or conjugate transposed before multiplication.

**A**: *m* rows by *k* columns

**B**: *k* rows by *n* columns

**C**: *m* rows by *n* columns

`alpha`: Real value used to scale the product of matrices A and B.

`beta`: Real value used to scale matrix C.

(Example: <https://software.intel.com/en-us/node/429920>)



## Matrix multiplication, standard algorithm

```
for (i=0;i<n;i++)
  for (j=0;j<m;j++)
  {
    tmp=0.0;
    for (k=0;k<p;k++)
      tmp += A[i][k] * B[j][k]; //B is transposed
    C[i][j]=tmp;
  }
```

## Matrix multiplication using MKL/BLAS library:

```
cblas_dgemm(CblasRowMajor,CblasNoTrans,CblasNoTrans,
            m, n, k, alpha, A, k, B, n, beta, C, n);
```

## Results

Lille (gcc compiler -O3): Matmult: 128s	BLAS: 0.9s
Vilje (icc compiler -O3): Matmult: 78.8 s	MKL: 2.48s



# Memory allocation.

Auto allocation of a memory.

Example:

```
{ // Inside a scop
    int a[10][10];
}
```

- The array is not reachable outside a scop and will be deleted when instruction pointer exit the scop. Scop is the program between {...}.
- The array will be stored into the stack. The stack has fast accessibility.
- The stack is limited. If you allocate more memory than available can result in a program crash due to stack overflow.
- For large memory allocation; use dynamic memory allocation.



## Dynamic memory allocation.

```
{  
    int n=1000; // Size of the array;  
    double *array; // Init array  
    array = (double *) malloc ( sizeof (double) * n );  
    ....  
    myfunction (n,array);  
    ....  
    free (array);  
}
```

- Dynamic memory allocated arrays will be stored in the heap.
- You can allocate all memory space.
- Heap has slower accessibility than the stack.
- The array will not be deleted when the instruction pointer go outside the scop. You have to use free(array);

